Effects of Size and Temperature on Metabolic Rate

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We derive a general model, based on principles of biochemical kinetics and allometry, that characterizes the effects of temperature and body mass on metabolic rate. The model fits metabolic rates of microbes, ectotherms, endotherms (including those in hibernation), and plants in temperatures ranging from 0°C to 40°C. Mass- and temperature-compensated resting metabolic rates of all organisms are similar: The lowest (for unicellular organisms and plants) is separated from the highest (for endothermic vertebrates) by a factor of about 20. Temperature and body size are primary determinants of biological time and ecological roles.

Metabolism sustains life. It is the process by which energy and materials are transformed within an organism and exchanged between the organism and its environment. Whole organism metabolic rate scales with the 3/4-power of body mass and increases exponentially with temperature (1, 2). The effect of temperature on a biological process is tradi-
tionally expressed as a $Q_{10}$, which quantifies temperature dependence across a limited temperature range (i.e., 10°C).

Size and temperature primarily affect metabolic rate through different mechanisms. Recently, a general model has been shown to explain the scaling of whole organism metabolic rate $B$ with body mass $M$, where $B \propto M^{3/4}$ so that mass-specific metabolic rate $B/M \propto M^{-1/4}$. This quarter-power scaling is based on the fractal-like design of exchange surfaces and distribution networks in plants (3) and animals (4). Temperature governs metabolism through its effects on rates of biochemical reactions. Reaction kinetics vary with temperature according to the Boltzmann's factor $e^{-E_i/kT}$, where $T$ is the absolute temperature (in degrees K), $E_i$ is the activation energy, and $k$ is Boltzmann's constant.

Metabolic rate is the consequence of many different biological reactions. So

$$B = \sum_i R_i$$

where the $R_i$ represents the rates of energy production via the individual reactions $i$ that comprise metabolism. Each reaction rate depends on three major variables: $R_i \propto (c$oncentration of reactants) (fluxes of reactants) (kinetic energy of the system). The first two terms, which are constrained by the rates of supply of substrates and removal of products, contain the majority of the body mass dependence. Because of allometric constraints on exchange surfaces and distribution networks (3, 4), the product of these two terms scales with body size as $M^{3/4}$. The third term contains the dominant temperature dependence, which is governed by the Boltzmann factor, $e^{-E_i/kT}$. This is valid within the limited range of "biologically relevant" temperatures between approximately 0°C and 40°C. This is the range in which organisms commonly operate within natural conditions. Near 0°C, metabolic reactions cease due to the phase transition associated with freezing water, and above approximately 40°C, metabolic reaction rates are reduced by the increasing influence of catalysis. We do not consider hyperthermophilies, specialized organisms that live at temperatures substantially hotter than 40°C.

The combined effects of body size and temperature on metabolic rate within the biologically relevant temperature range can therefore be well approximated by

$$B \propto M^{3/4} e^{-E_i/kT}$$

Here $E_i$ represents an average activation energy for the rate-limiting enzyme-catalyzed biochemical reactions of the system. Because, for each taxon, $B/M^{3/4} = B_0$ is approximately independent of $M$, almost all of the temperature variation is contained in the normalization term, $B_0$.

$$B_0 \sim e^{-E_i/kT}$$

(2)

Because the biochemistry of metabolism is common to aerobic organisms, we predict that plotting mass-normalized metabolic rates $[\ln(B/M)]$ as a function of $1/T$ for different taxonomic or functional groups should yield similar straight lines with slopes $a = -E_i/kT$.

Furthermore, we predict that the values of $E_i$ obtained from these plots will fall within the range of measured activation energies for metabolic reactions. Because these activation energies vary between 0.2 and 1.2 eV with an average of approximately 0.6 eV (5, 6), the slope of these lines should have a universal value of approximately -7.40 K.

We evaluated these predictions using resting metabolic rates as a function of temperature and body mass for a variety of organisms: aerobic microbes, plants, multicellular invertebrates, fishes, amphibians, reptiles, birds, and mammals (Fig. 1) (7). Plots of these data are well fit by straight lines, all with similar slopes and intercepts. This supports the first prediction. Furthermore, the average activation energies extracted from the slopes give $E_i = 0.41 - 0.74$ eV with a mean for all groups of 0.63 eV. This supports the second prediction. Figure 1 suggests that as a first approximation the metabolic rates of all organisms are a single, general function of body size and temperature. An expression for the dependence of metabolic rate on body size and temperature can be derived from Eq. 2 by noting that the value of $B_0$ at some temperature $T$ can be related to its value at some other temperature $T_0$ by

$$B_0(T) = B_0(T_0) e^{-E_i/(kT - kT_0)}$$

$$= B_0(T_0) e^{-E_i/(k(T - T_0))}$$

(3)

Combined with Eq. 1 this leads to

$$B = B_0(T) M^{3/4} = B_0(T_0) M^{3/4} e^{E_i/k(T - T_0)}$$

where $T_c = T - T_0$. The term $e^{E_i/k(T - T_0)}$ which describes the "universal temperature dependence" (UTD) of biological processes. Equation 3 allows metabolic rates of different organisms to be compared independently of body mass and temperature by comparing their values of $B_0(T_c)$ normalized with some standard temperature, $T_c$ (often 20°C).

Equation 3 also expresses the temperature dependence in terms of degrees Celsius by choosing $T_0$ to be the freezing point of water (~273 K), in which case $T_c = T - T_0$ defines temperature in degrees Celsius. Biologists would be better served by quantifying temperature-dependence in terms of the UTD rather than the traditional $Q_{10}$ factor, which is defined by the equation

$$\frac{B_0(T)}{B_0(T_0)} = [Q_{10}]^{|T - T_0|/10} = [Q_{10}]^{T/10}$$

(4)

with $Q_{10}$ considered a constant, which is independent of temperature. From Eq. 3, however, we see that $Q_{10}$ must, in fact, have a temperature dependence given by

$$Q_{10} = e^{10E_i/kT_0} = e^{10E_i/(kT_0)}$$

(5)

In other words, biological processes do not generally depend purely exponentially on

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**Fig. 1.** Effect of temperature (1000/degrees K) on mass-normalized resting metabolic rate ($B_0$ in W/g/m^2) for unicells (A), plants (B), multicellular invertebrates (C), fish (D), amphibians (E), reptiles (F), and birds and mammals (G). Birds (gray symbols) and mammals (open symbols) are shown at normal body temperatures (triangles) and during hibernation or torpor (squares). Data sources listed on Science Online (7).
temperature (in degrees Celsius). Calculating temperature dependence using Eq. 4 with a constant value of $Q_{10}$ introduces an error that can be as much as 15% over the "biologically relevant" temperature range. Using the UTD not only avoids this error, but also expresses temperature dependence in terms of the activation energy $E_a$ and Boltzmann's constant $k$, thereby linking whole-organism metabolism directly to the kinetics of the underlying biochemical reactions.

Because biological times are the reciprocals of biological rates per unit mass, Eq. 1 can be rewritten to give a general expression for biological time ($t_b$) in terms of body size and temperature

$$t_b \propto M^{-1/4} e^{E_a/T}$$

Eq. 6 should apply to all biological times, from times of biochemical reactions and cell cycles to developmental times and life-spans. Thus, we predict that plots of $\ln(t_b)$ vs. $M^{-1/4}$ as a function of $1000/T$ should yield straight lines with slopes identical in magnitude but opposite in sign to the plots of $\ln(t_p)$ as a function of $1000/T$ for each group (Fig. 1). Plots of life-spans ($L_S$) of fish and aquatic invertebrates of varying body sizes measured at different constant temperatures support this prediction (Fig. 2) (7). The slopes for life-span are 6.37 and 6.50 for fish and aquatic invertebrates, respectively, compared with slopes of $-5.02$ and $-9.15$ for metabolic rate. The approximately opposite slopes mean that over the lifetime of these animals a unit of mass uses approximately the same quantity of energy, regardless of body size and temperature.

This is not meant to imply that Eq. 1 can account for all variation in biological rates and times. There is residual variation about the lines in Fig. 1 that reflects differences among species. Moreover, the data that we compiled are for resting metabolic rates. Rates of metabolism for endotherms during maximal aerobic activity can be as much as 8- to 10-fold greater than those at rest (8).

Furthermore, in response to stressful environmental conditions, some organisms have metabolic rates below normal resting levels (e.g., diapause, anhydrobiosis) (9). We regard Eq. 1 as the zeroth-order model that describes the effects of size and temperature as primarily. Other, secondary factors are required to explain the remaining variation within and between groups.

The general application of Eq. 1 is demonstrated by the diversity of organisms depicted in Fig. 1. The unicells include protoists, algae, and bacteria. The data for plants include not only whole plants, but also fruits, storage organs (tubers, bulbs), and hydrated seeds. Botanists rarely measure rates of whole-plant photosynthesis or respiration as a function of "body" size and temperature [but see (10)]. These results suggest that metabolic rates of plants are similar to those of unicellular organisms and invertebrate animals. The data for birds and mammals include not only resting individuals of many species at normal body temperatures, but also individuals in hibernation or torpor at lower body temperatures. These last data imply that the lower metabolic rates of torpid endotherms can be attributed to temperature, as long as body temperatures approximate ambient temperatures; there is no need to invoke other mechanisms to reduce metabolic rate during torpor (11).

The primary effects of size and temperature and the residual variation due to other factors can be shown by comparing metabolic rates as a function of temperature and body mass (Fig. 3). Three results are apparent. First, the slopes are similar (Fig. 3A) for all groups except fish and amphibians, which appear to have slopes which are slightly less negative, and consequently also have lower intercepts. Second, the average relations for the different groups are offset somewhat (Fig. 3A). The maximum difference separating any of the groups, unicells and plants from birds and mammals, is approximately $e^3$ or 20-fold. Third, these differences are small compared with variation in measured values within the groups (Fig. 3B). The data points for each group in Fig. 1 overlap broadly across groups, calling attention to the similarity in metabolic rates of all organisms.

This similarity is perhaps best depicted by plotting whole-organism metabolic rates, corrected to a common temperature of 20°C, as a function of body mass (12).
This allows a comparison of temperature-standardized resting metabolic rates with Hemmingsen's classical study (1) (Fig. 4). Hemmingsen's work implies that ectotherms, endotherms, and unicells have distinctively different, nonoverlapping metabolic allometries. He argues that this suggests three major steps in the evolution of animal metabolism. The data in Fig. 4 show that this is an oversimplification. Temperature-standardized metabolic rates do not differ among unicells, invertebrates, and plants, but the rates for ectothermic vertebrates (fishes, amphibians, and reptiles) are slightly higher, and the rates for endothermic birds and mammals are slightly higher still. So instead of these groups having no overlap and differing by a factor of approximately 225 as suggested by Hemmingsen, there is extensive overlap with the average metabolic rates of unicells and plants separated from those of birds and mammals by about 20-fold.

Thus, metabolic rate—the rate at which organisms transform energy and materials—is governed largely by two interacting processes: the Boltzmann factor, which describes the temperature dependence of biochemical processes, and the quarter-power allometric relation, which describes how biological rate processes scale with body size. Here we show that using $Q_{10}$ can introduce substantial error and that the temperature dependence of metabolic rate is relatively constant across a range of temperatures from 0 to 40°C. Application of the UTD to data on biological rate processes should reveal when the observed variation in response to temperature can be explained parsimoniously by Eq. 1, and when some additional biological mechanism is required. Emphasis on how metabolic rates depend primarily on body size and temperature promises to contribute to understanding how microbes, plants, and animals control the fluxes and storage of energy and materials on scales from local ecosystems to the biosphere (13, 14).

References and Notes
2. M. Kleiber, Hilgardia 6, 315 (1932).
7. Metabolic rates were measured as resting rates using oxygen consumption in animals and unicells, and oxygen consumption or carbon dioxide production in plants. A respiratory coefficient of 1 was used to convert CO₂ production to O₂ consumption in plants. A density of 1.43 g/l for O₂ and 1.97 g/l for CO₂ was used to convert various units to ml/hour. A factor of 0.0056 W/kg was used to convert ml/hour to W/kg. Unicell mass was sometimes estimated from volume using a density of 1 g/ml. Metabolic rates of fish were stipulated as standard rates. Sources for all data presented in this paper, and statistics for regressions presented in Web fig. 1 and table 1 are available on Science Online at www.sciencemag.org/cgi/content/full/293/5538/2248/DC1.
12. Metabolic rates in Fig. 4 were standardized to 20°C using the equation $B_{\text{MRC}} = B_{\text{MRC}}(270-10)^{10}$ where $t$ is body temperature and $k$ is the slope of the line for each species group from Fig. 1.
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